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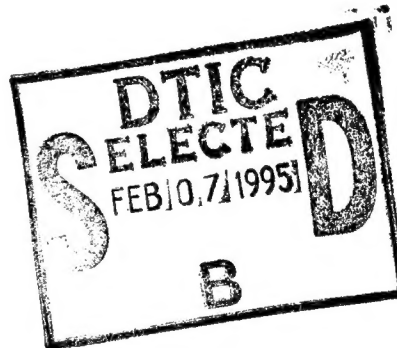


# Computational Fluid Dynamics (CFD) Simulation of Test Chamber and Smoke-Generating Device

Michael J. Nusca

ARL-TR-663

January 1995



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13. ABSTRACT (Maximum 200 words)  The U.S. Army Research Laboratory (ARL) has completed an initial investigation of the flow field within a typical U.S. Army Edgewood Research, Development, and Engineering Center (ERDEC) test chamber via numerical simulation. The ERDEC test chamber is designed to mix compressor-driven airflow with gas/solid effluent from a test article placed inside the chamber. An example of such a test article is a smoke generator, or smoke pot. Simulation of this flow utilized ARL computational fluid dynamics (CFD) codes that include multispecies chemical kinetics. Numerical solutions of the gas flow and effluent concentration distributions in the test chamber were generated for operating times up to 4.5 min. Numerical simulations reveal that certain values of chamber through-flow induce flow patterns within the chamber that are dominated by rotating vortices. This flow pattern increases the effluent residence time in the chamber as well as the mixing of gas/particulate from the test article with air. As a result, pockets of high effluent concentration can form in the chamber. Graphical results with discussion are presented.				
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## 1. INTRODUCTION

The U.S. Army Research Laboratory (ARL) completed an initial investigation of the flow field within a typical test chamber operated by the Army Edgewood Research, Development and Engineering Center (ERDEC). The ERDEC test chamber is designed to mix compressor-driven airflow with gas/solid effluent from a test article placed inside the chamber. An example of such a test article is a smoke generator, or smoke pot, commonly used on the battlefield to provide a means of obscurant. During the test, the air/effluent flow field is exhausted from the test chamber for analysis. In order to simulate this flow, the ARL applied computational fluid dynamics (CFD) codes that include multispecies chemical kinetics as well as multiphase (particulate) submodels. These codes were developed at ARL to numerically solve the Navier-Stokes equations and simulate the chemically reacting, multiphase flow field in gun propulsion systems. This code has been used successfully for other applications at ARL (Nusca 1989, 1991, 1993).

Application of the code to the present study involved generating a computational mesh that covered the chamber interior as well as specifying proper boundary conditions on the chamber walls, chamber top (air inflow), chamber exit (outflow), and test article (effluent outflow), as depicted in Figure 1. The governing equations, boundary conditions, and solution method are outlined in this report. Numerical solutions of the gas flow and effluent concentration distributions in the test chamber were generated for operating times up to 4.5 min. Graphical results with discussion are presented in this report. Numerical simulations reveal that certain values of chamber through-flow induce flow patterns within the chamber that are dominated by vortices. This flow pattern increases the effluent residence time in the chamber as well as the mixing of gas/particulate from the test article with air. The test article effluent jet feeds effluent into this vortical motion, and only that flow that is trapped near the chamber floor is drawn out of the chamber. Pockets of high effluent concentration can form in the chamber.

## 2. GOVERNING EQUATIONS

For purposes of producing a timely initial investigation, the cylindrical test chamber was modeled as two-dimensional (2D). The governing equations are written in Cartesian coordinates with velocity components  $u$  and  $v$  for the  $x$  (along chamber floor) and  $y$  (along chamber height) directions, respectively (see Figure 1). The Reynolds-Averaged Navier-Stokes (RANS) equations describe the 2D reacting gas flow ( $N$  species mixture) in the chamber given conditions at the boundaries of the geometry. These partial differential equations describe the time ( $t$ ) evolution of the dependent variables of velocity ( $u, v$ ), pressure

(p), mixture density ( $\rho$ ), species mass fraction ( $\sigma_i$ , for  $i = 1$  to  $N$  species), internal energy ( $e$ ), temperature ( $T$ , derived from energy), and viscous shear stresses ( $\tau$ ).

$$\frac{\partial W}{\partial t} + \frac{\partial (F_1 - G_1)}{\partial x} + \frac{\partial (F_2 - G_2)}{\partial y} = \Omega. \quad (1)$$

$$W = [e, \rho, \rho u, \rho v, \rho \sigma_1, \dots, \rho \sigma_{N-1}].$$

$$F_1 = [(e+p) u, \rho u, \rho u^2 + p, \rho uv, \rho u \sigma_1, \dots, \rho u \sigma_{N-1}].$$

$$F_2 = [(e+p) v, \rho v, \rho vu, \rho v^2 + p, \rho v \sigma_1, \dots, \rho v \sigma_{N-1}].$$

$$\Omega = [0, 0, 0, 0, \sum_k \omega_{1k}, \dots, \sum_k \omega_{(N-1)k}].$$

$$G_1 = \left[ \kappa_m \frac{\partial T}{\partial x} + \sum_i \rho D (h_i - h_N) \frac{\partial \sigma_i}{\partial x} + u \tau_{xx} + v \tau_{xy}, 0, \tau_{xx}, \tau_{xy}, \rho D \frac{\partial \sigma_1}{\partial x}, \dots, \rho D \frac{\partial \sigma_{N-1}}{\partial x} \right].$$

$$G_2 = \left[ \kappa_m \frac{\partial T}{\partial y} + \sum_i \rho D (h_i - h_N) \frac{\partial \sigma_i}{\partial y} + u \tau_{yx} + v \tau_{yy}, 0, \tau_{yx}, \tau_{yy}, \rho D \frac{\partial \sigma_1}{\partial y}, \dots, \rho D \frac{\partial \sigma_{N-1}}{\partial y} \right].$$

The shear stress terms are given by

$$\tau_{xx} = 2\mu_m \frac{\partial u}{\partial x} - \frac{2\mu_m}{3} \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right), \tau_{yy} = 2\mu_m \frac{\partial v}{\partial y} - \frac{2\mu_m}{3} \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right), \tau_{yx} = \mu_m \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right).$$

In these equations,  $\sigma_i$  and  $\omega_i$  are the mass fraction and chemical production terms for the  $i^{\text{th}}$  species. For the present application, finite-rate chemical production terms were not used. Chemical reaction was modeled as an infinitely fast, one-step, unidirectional (i.e., forward) reaction of smoke pot effluent ( $i = 1$ ) and air ( $i = 2$ ) to form product ( $i = 3$ ) for stoichiometric air/effluent ratio of 0.17 and effluent density above  $50 \text{ g/m}^3$ . The reaction temperature was taken as  $680^\circ \text{ C}$ .

Effluent + Air  $\rightarrow$  Product

$$\frac{\omega_1}{M_1} = -k_f \frac{\rho \sigma_1}{M_1} \frac{\rho \sigma_2}{M_2}, \quad \frac{\omega_2}{M_2} = -k_f \frac{\rho \sigma_1}{M_1} \frac{\rho \sigma_2}{M_2}, \quad \frac{\omega_3}{M_3} = +k_f \frac{\rho \sigma_1}{M_1} \frac{\rho \sigma_2}{M_2}.$$

$$k_f = 1 \times 10^{20}.$$

The temperature dependence of the species viscosity,  $\mu_i$ , and thermal conductivity,  $\kappa_i$ , can be modeled using Sutherland's law (White 1974),

$$\frac{\mu_i}{\mu_{oi}} = \left( \frac{T}{T_{op}} \right)^{3/2} \frac{T_{op} + S_\mu}{T + S_\mu}, \quad \frac{\kappa_i}{\kappa_{oi}} = \left( \frac{T}{T_{ok}} \right)^{3/2} \frac{T_{ok} + S_\kappa}{T + S_\kappa}.$$

The terms  $\mu_o$ ,  $T_o$ , and  $S$  can vary with species but were assumed to be constant with values of  $S_\mu = 199$  R,  $T_{op} = 491.6$  R,  $\mu_o = 0.1716$  mP,  $S_\kappa = 350$  R,  $T_{ok} = 491.6$  R,  $\kappa_o = 0.0139$  BTU/h-ft-R. The mixture viscosity and thermal conductivity (mixture quantities are denoted by subscript m) are determined using Wilke's law (Wilke 1950), denoting f as  $\mu$  or  $\kappa$ ,

$$f_m = \sum_i \left[ X_i f_i \left( \sum_j X_j \phi_{ij} \right)^{-1} \right], \quad \phi_{ij} = \frac{1}{\sqrt{8}} \left( 1 + \frac{M_i}{M_j} \right)^{-1/2} \left[ 1 + \left( \frac{f_i}{f_j} \right)^{1/2} \left( \frac{M_j}{M_i} \right)^{1/4} \right]^2,$$

where  $X_i$  and  $M_i$  are the mole fraction ( $X_i = \rho \sigma_i / M_i$ ) and molecular weight of the  $i^{\text{th}}$  species, respectively ( $M_1 = 97.94$ ,  $M_2 = 28.8$ , and  $M_3 = 63.37$  g/mole). Fick's law (White 1974) is used to relate the mixture diffusivity to the mixture viscosity through the Schmidt number,  $Sc = \mu_m / (\rho D)$ , assumed unity. The specific heat at constant pressure of each species (per mass) is generally given by the following fourth-order polynomial curve fit (Drummond, Rogers, and Hussaini 1987):

$$\frac{c_{p_i}}{R_i} = A_i + B_i T + C_i T^2 + D_i T^3 + E_i T^4.$$

For the present study,  $c_p$  was assumed constant with values  $c_{p1} = 0.2878$ ,  $c_{p2} = 0.238$ , and  $c_{p3} = 0.1277$  cal/g°C. The mixture pressure (equation of state), enthalpy, total energy per unit volume,

and ratio of specific heats are given by ( $R_u$  is the universal gas constant and  $\Delta H_f$  is the heat of formation for species  $i$ )

$$p = \sum_i p_i = \rho T R_u \sum_i \frac{\sigma_i}{M_i} ,$$

$$h = \sum_i \sigma_i \int^T c_{p_i} dT + \sum_i \sigma_i \Delta H_{f_i} ,$$

$$e = \frac{p}{\gamma-1} + \rho \frac{(u^2 + v^2)}{2} + \sum_i \rho \sigma_i \Delta H_{f_i} ,$$

$$\gamma = 1 + \left[ \frac{c_{p_m}}{R_u \sum_i (\sigma_i / M_i)} - 1 \right]^{-1} ,$$

and

$$c_{p_m} = \frac{1}{T} \sum_i \sigma_i \int^T c_{p_i} dT .$$

An algebraic turbulence model (Bradshaw, Cebeci, and Whitelaw 1981) was used. In this model, the eddy viscosity,  $\mu_t$ , is computed assuming that the viscous layer consists of an inner and an outer component. The inner region follows the Prandtl mixing length formulation based on a prescribed characteristic length scale,  $L$ , a boundary layer intermittency factor,  $\epsilon$  (having a value of 0 for laminar, 1 for turbulent flows, and a function of  $x$  for transitional flows), the displacement thickness of the layer,  $\delta$ , and a constant,  $a$ .

$$(\mu_t)_{\text{inner}} = L^2 y \left\| \frac{\partial u}{\partial y} \right\| , \quad 0 \leq y \leq y_c .$$

$$(\mu_t)_{\text{outer}} = a u_e \left\| \delta \right\| \epsilon , \quad y_c \leq y \leq y_e .$$

Here,  $y_c$ , is a prescribed, small distance from the solid boundary, and  $y_e$  is the edge of the viscous layer. Further details can be obtained from Bradshaw, Cebeci, and Whitelaw (1981). The fluid viscosity is then  $\mu = \mu_m(T) + \mu_t$ , where  $\mu_m(T)$  is obtained using Sutherland's law and Wilke's law.

### 3. BOUNDARY CONDITIONS AND INITIAL CONDITIONS

The boundaries of the test chamber (see Figure 1) are the air inlet at the top (roof), the exit port on the chamber floor (connected by ducts to the wind tunnel fan), and the vertical walls. The smoke pot is placed on the chamber floor, near the chamber exit port. Since the governing equations are elliptic (low-speed flow), conditions along these boundaries must prescribe values of the dependent variables, the gradient of the dependent variables in the boundary-normal direction, or an algebraic relation which connects the values of the dependent variables to the normal component of velocity.

At the air inlet, x-direction profiles of all dependent variables,  $p$ ,  $u$ ,  $v$ ,  $\sigma$ ,  $T$ , and  $\rho$ , are specified. It is assumed that the flow at the inlet consists of air and that convection/diffusion of effluent to the chamber top is not permitted to exit the chamber. By mass conservation, the inlet flow velocity was specified as  $u = .062$  ft/s, and a parabolic-shaped profile was assumed.

The exit port velocity was specified as  $u = 2.96$  ft/s (5,380 l/min) with a parabolic-shaped profile. Boundary-normal gradients of all dependent variables at the exit plane are zero. Mass that exits the port is not assumed to reenter.

The no-slip/no-penetration condition ( $u = v = 0$ ) is applied to the solid chamber and smoke pot walls. The walls are assumed to be adiabatic (i.e., normal derivative of  $T$  set to zero). The normal gradient of all mass fractions,  $\partial\sigma_i/\partial n$ , are also set to zero.

The top of the smoke pot was assumed to be a constant mass flux source of effluent with  $u = 12.7$  ft/s,  $T = 320^\circ$  C,  $M_1 = 97.94$  g/mole, and  $c_p = 0.2878$  cal/g $^\circ$  C.

### 4. COMPUTATIONAL ALGORITHM

Equation (1) can be reduced to a successive-substitution formula for a general dependent variable,  $W$ , at each node on the computational grid. Central finite-differences are used for the diffusive (arrays  $G_1$

and  $G_2$ ) and source terms (array  $\Omega$ ) and upwind differences for the convective terms (arrays  $F_1$  and  $F_2$ ). Using upwind differencing in the species conservation equations (i.e.,  $W = \rho\sigma_i$ ) reduces the occurrence of negative species mass fractions in mixing layers. The resulting system of equations for the entire grid is solved using a Gauss-Seidel relaxation scheme. Each iteration cycle is made up of  $J$  subcycles, where  $J$  is the number of equations being considered. In each subcycle, grid points are scanned row by row, and a single variable is updated. When all subcycles are completed, a new iteration cycle in which the values of the variables from the latest iteration are immediately used is started. This is consistent with the Gauss-Seidel methodology. Convergence is satisfied when the greatest relative change in any flow variable is smaller than a prescribed tolerance. See Nusca (1989, 1991) for further details.

## 5. RESULTS AND DISCUSSION

Figure 1 shows the computational grid used to discretize the chamber interior. The number of grid nodes in the  $x$  and  $y$  directions are 75 and 50, respectively (3,750 nodes total). Grid node clustering was used to resolve flow gradients near the smoke pot.

The simulation was run for approximately 1 min to establish steady flow in the chamber before the smoke pot was activated. Figure 2 shows the streamline (contour lines of constant stream function) patterns. Note that a large counterclockwise vortex resides to the upper left of the smoke pot (established by flow from the chamber inlet that must turn at the chamber floor) and that a smaller clockwise vortex resides over the smoke pot (established by flow rising in the vertical direction that is turned by the chamber inlet flow at the top).

Figures 3, 4, 5, and 6 show the flow streamline pattern after 1, 2, 3, and 4 min of smoke pot operation, respectively. Initially, flow from the smoke pot rises toward the chamber top, establishing two small vortices near the pot, rotating in opposite directions. At later times, the flow settles into a large counterclockwise vortex offset from the centerline of the chamber and fed by the smoke pot jet. Flow entrained in the chamber exit port is limited to that trapped near the chamber floor. Figure 7 shows the flow streamline pattern at 4.5 min, which is 0.5 min after the smoke pot has ceased operation. The vortex has reduced in size and is centered between the vertical chamber walls.

Figures 8–12 and Figures 13–17 show contours of smoke pot effluent mass fraction,  $\sigma_1$ , (mass of effluent/total mass) and effluent density (product of mass fraction and mixture density), respectively, at



times 1–4.5 min. At early times, effluent concentrations are high in the smoke pot jet. At later times, the effluent is entrained in the chamber vortex and diffused to smaller concentrations. Even at later times, pockets of high concentration ( $50 \text{ g/m}^3$  or greater) can be noted. The flow pattern is not greatly disturbed by the chamber exit port on the floor. Figures 12 and 17 show the effluent mass fraction and density at 4.5 min, 0.5 min after flow from the smoke pot has been stopped. The chamber vortex has swept effluent into the vicinity of the smoke pot where it becomes trapped at large concentration levels.

## 6. CONCLUSIONS

Due to the low-vertical flow velocity (0.06–2.7 ft/s) through the chamber induced by the small chamber exit port on the floor, the natural flow pattern in the chamber is one that is dominated by rotating vortices. This pattern increases the flow residence time in the chamber and mixes gases from the smoke pot with air (similar to a "well-stirred reactor"). The smoke pot jet feeds effluent into this vortical motion, with only that flow that is trapped near the chamber floor exiting the chamber. As a result, effluent is allowed to form pockets of high concentration that may chemically react with the fresh-air supply fed from the chamber inlet (i.e., top). After the smoke pot ceases operation, the chamber vortex concentrates effluent near the chamber wall. A larger chamber exit port and forced exit velocity (controlled by the wind tunnel fan) may assist in breaking these vortices and evacuating the chamber at the higher rate. The increased chamber through-flow should be sufficient to turn the smoke pot jet toward the exit. Numerical simulations aimed at predicting this effect have not been pursued.

The numerical simulations, results, discussions, and conclusions reached in this report are subject to the assumptions used in the model and the information supplied to the model in the form of boundary conditions. While the confidence level in the model is high (based on performance in simulating other problems), further studies that test model sensitivity to the supplied boundary conditions should be conducted. A full three-dimensional simulation should be conducted to model the perforated chamber top wall, in addition to three discrete smoke pot exit holes as well as flow obstructions (i.e., pipes) in the chamber. These are thought to represent secondary effects in the simulation of unknown final effect on the results.

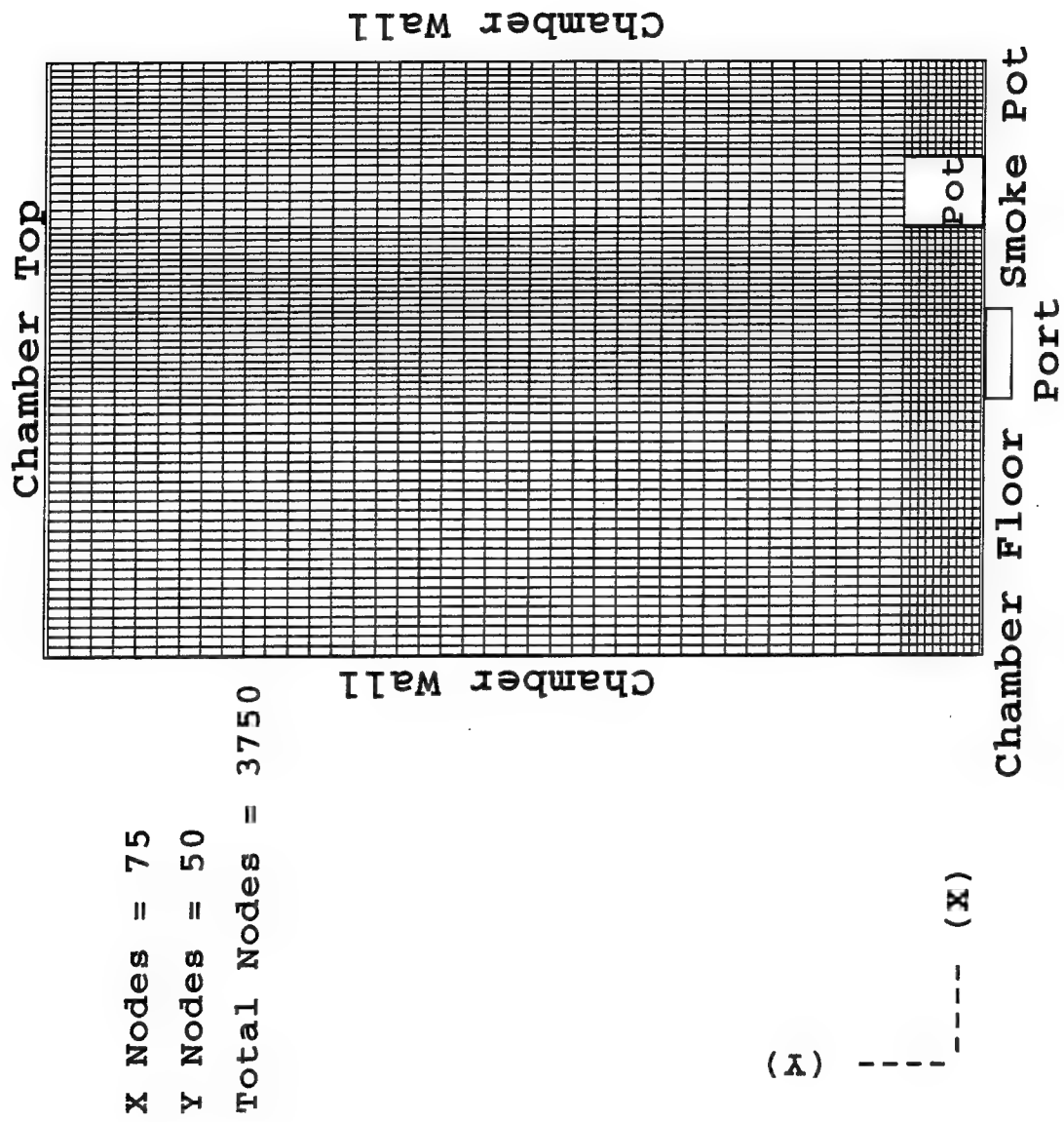


Figure 1. Schematic of test chamber and smoke pot showing computational grid.

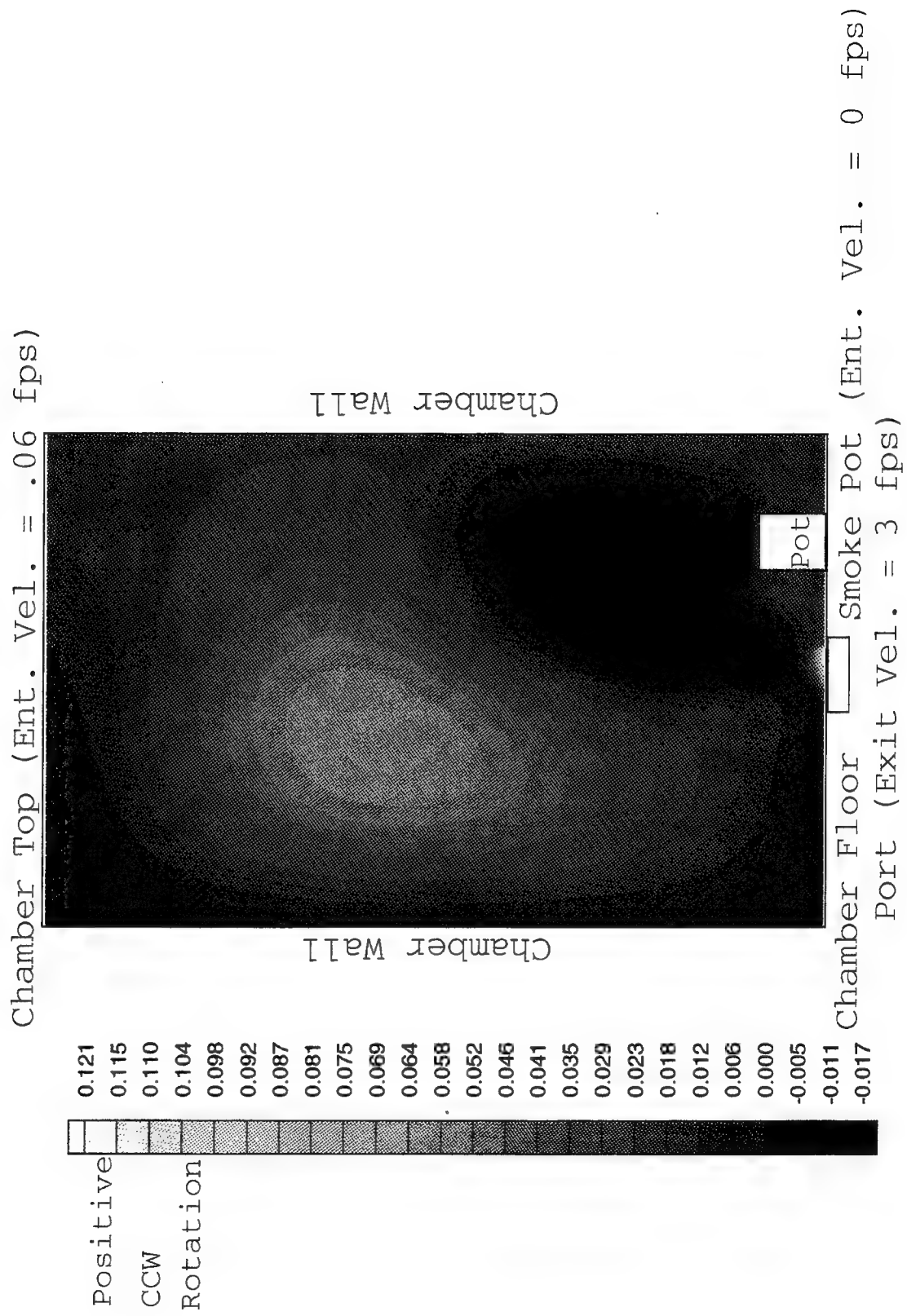


Figure 2. Stream function contours before smoke pot operation.

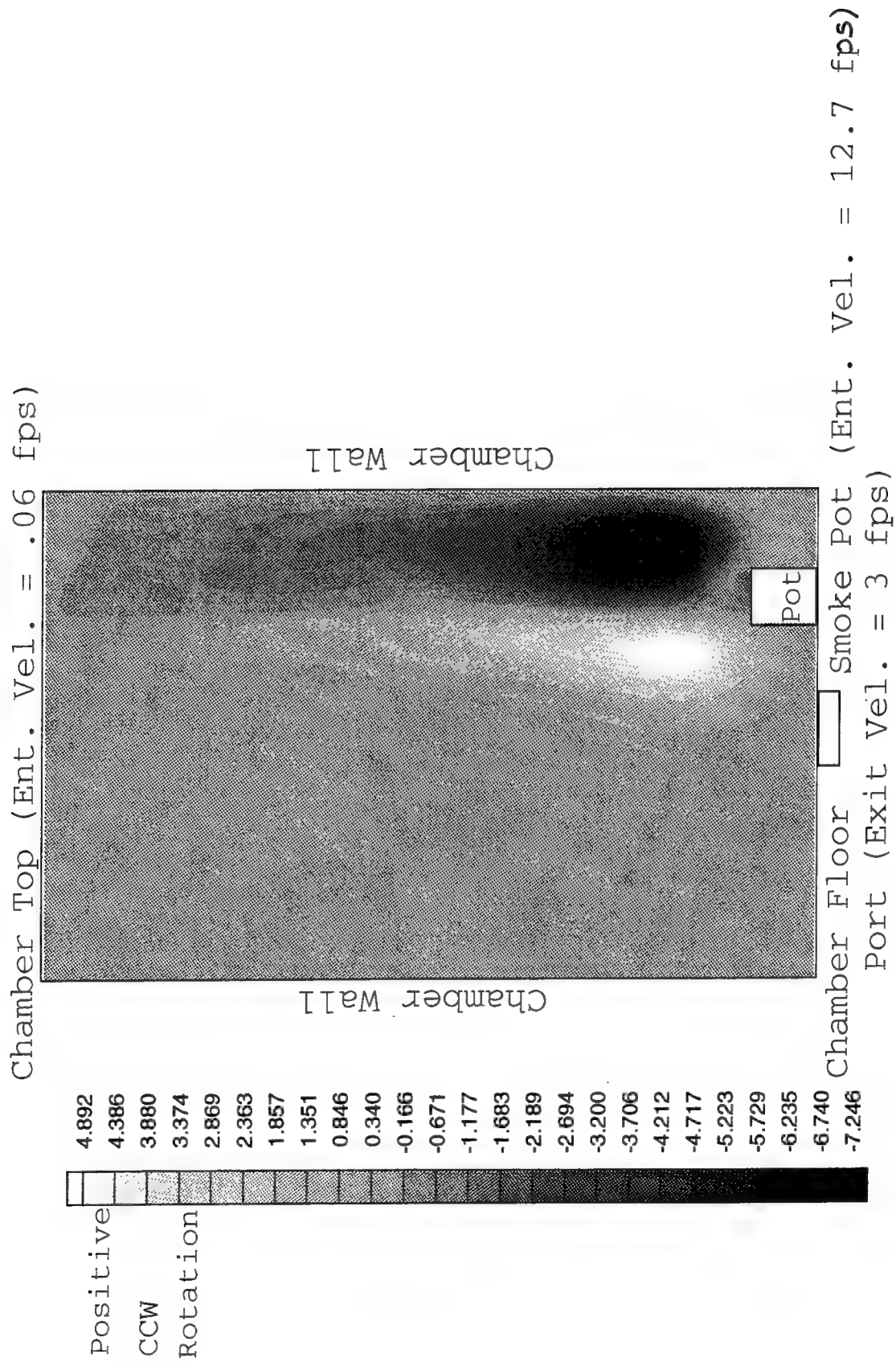


Figure 3. Stream function contours 1.0 min after smoke pot startup.

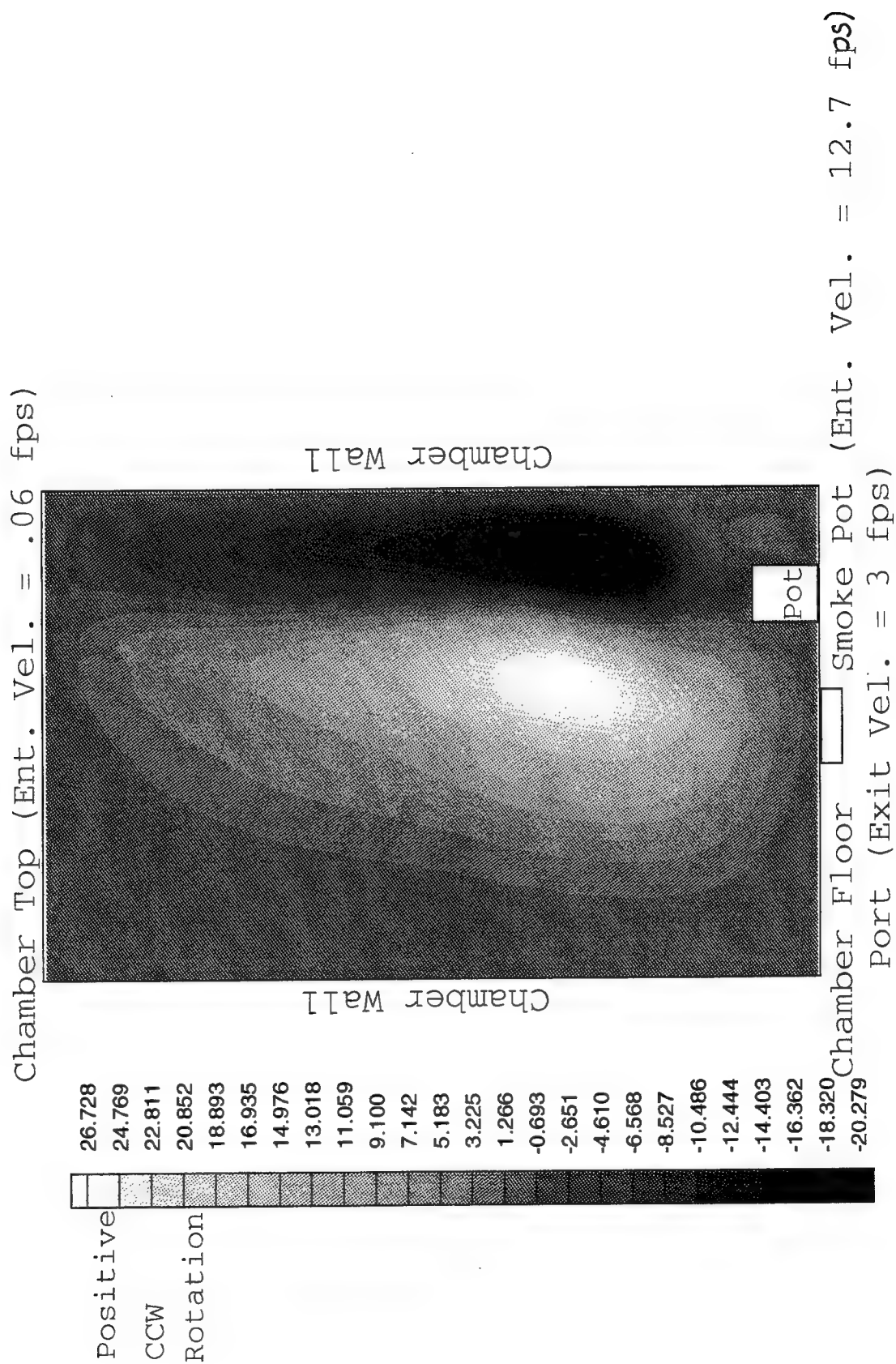


Figure 4. Stream function contours 2.0 min after smoke pot startup.

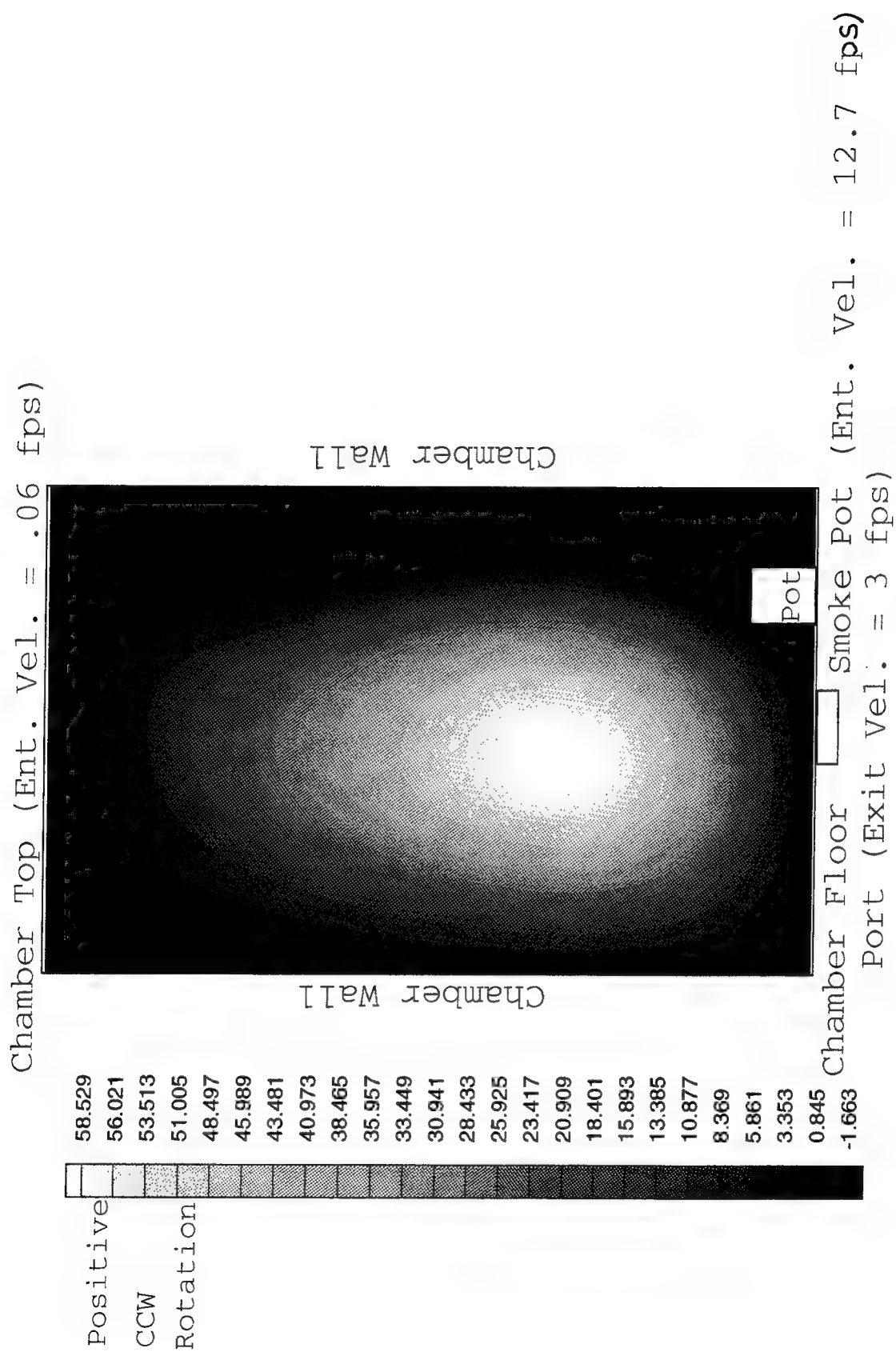


Figure 5. Stream function contours 3.0 min after smoke pot startup.

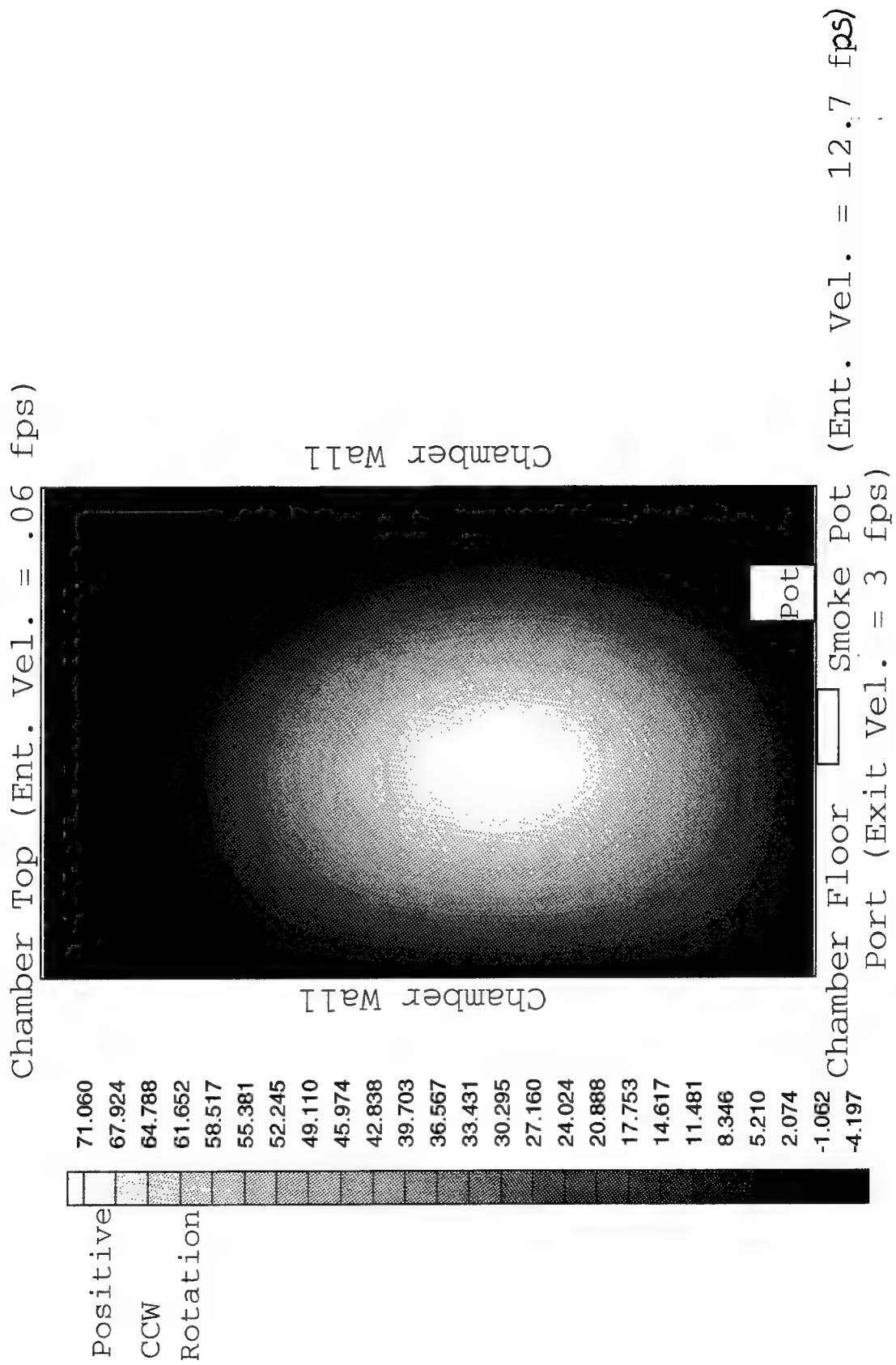


Figure 6. Stream function contours 4.0 min after smoke pot startup.

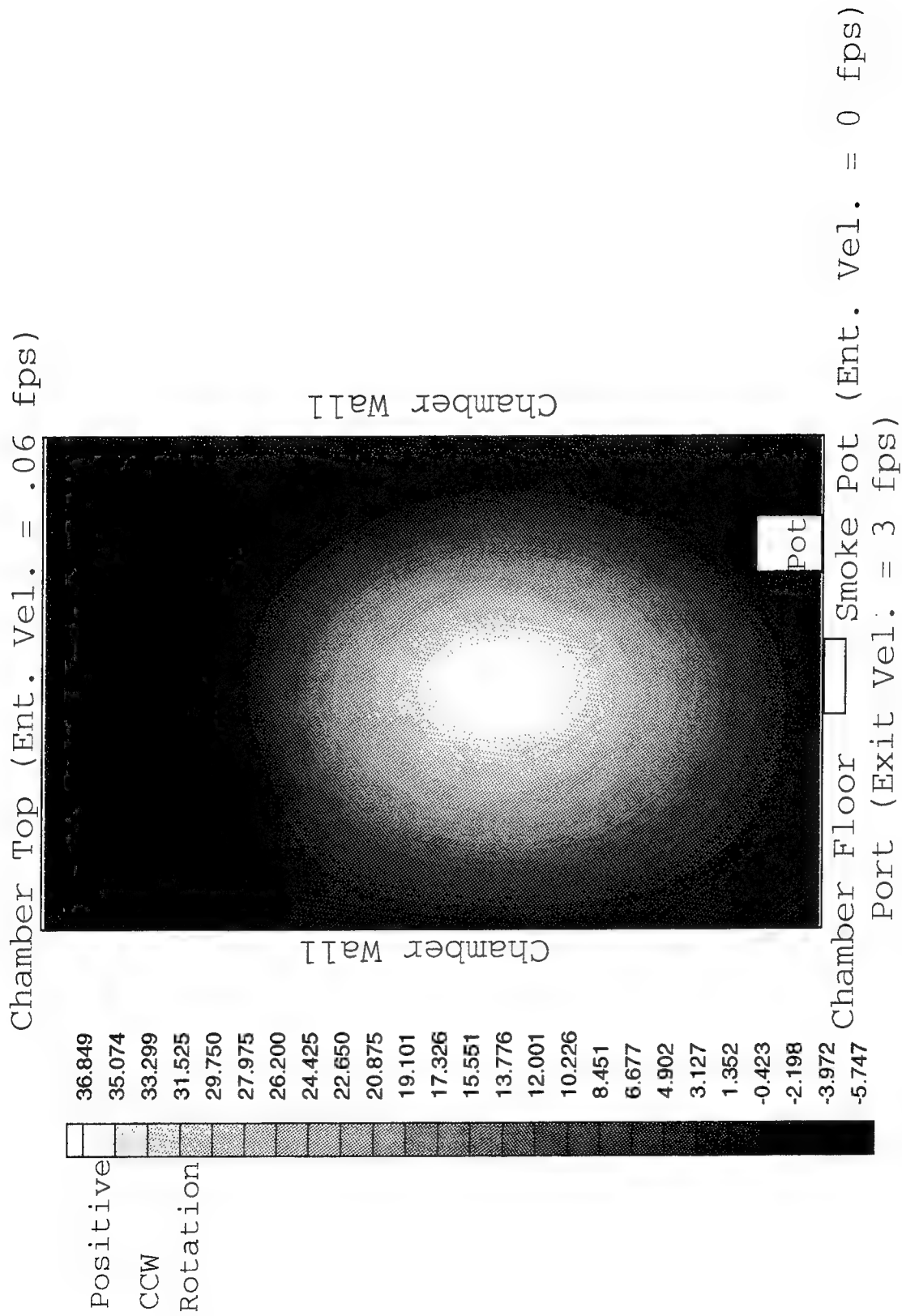


Figure 7. Stream function contours 4.5 min after smoke pot startup, 0.5 min after smoke pot termination.



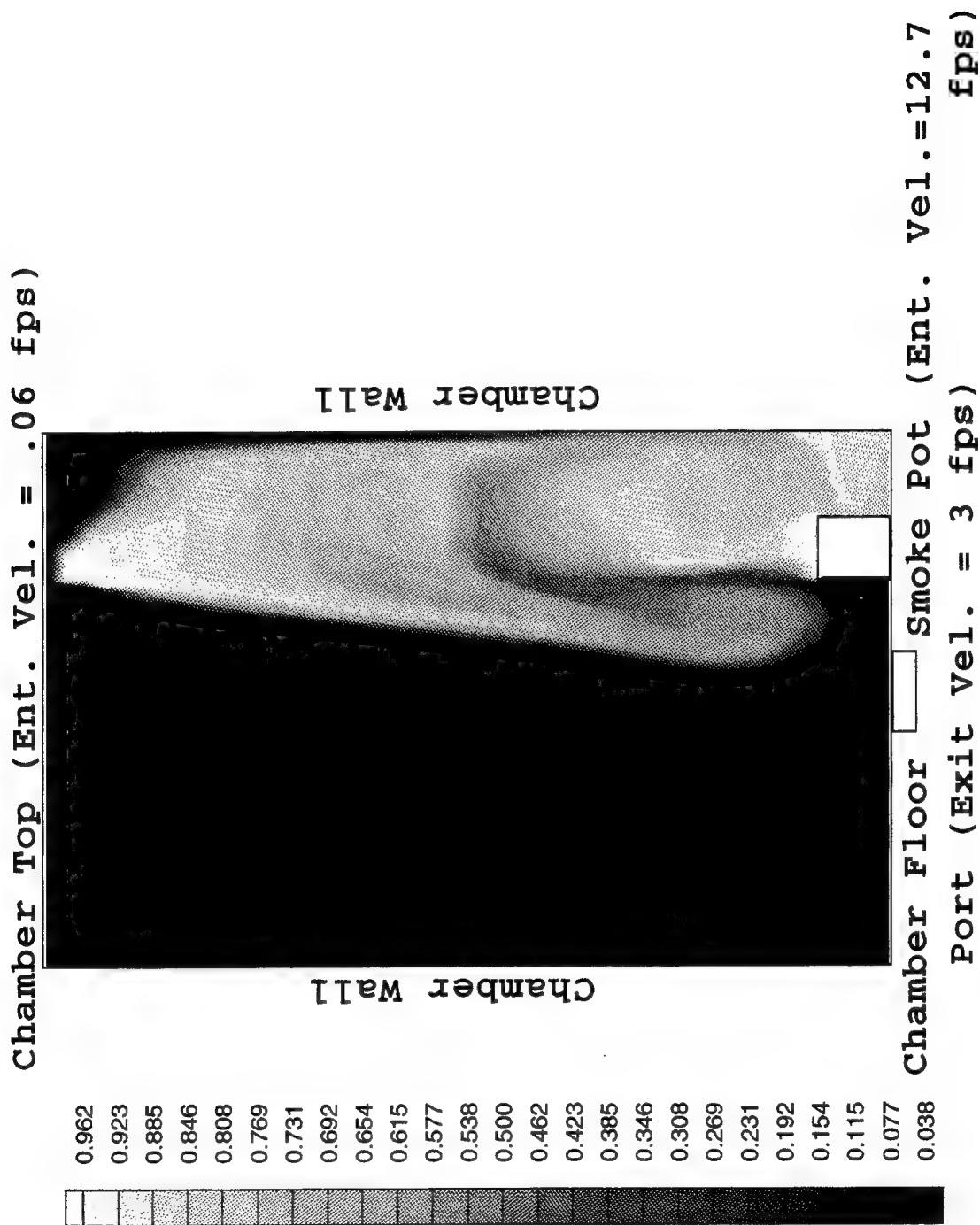


Figure 8. Effluent mass fraction contours 1.0 min after smoke pot startup.

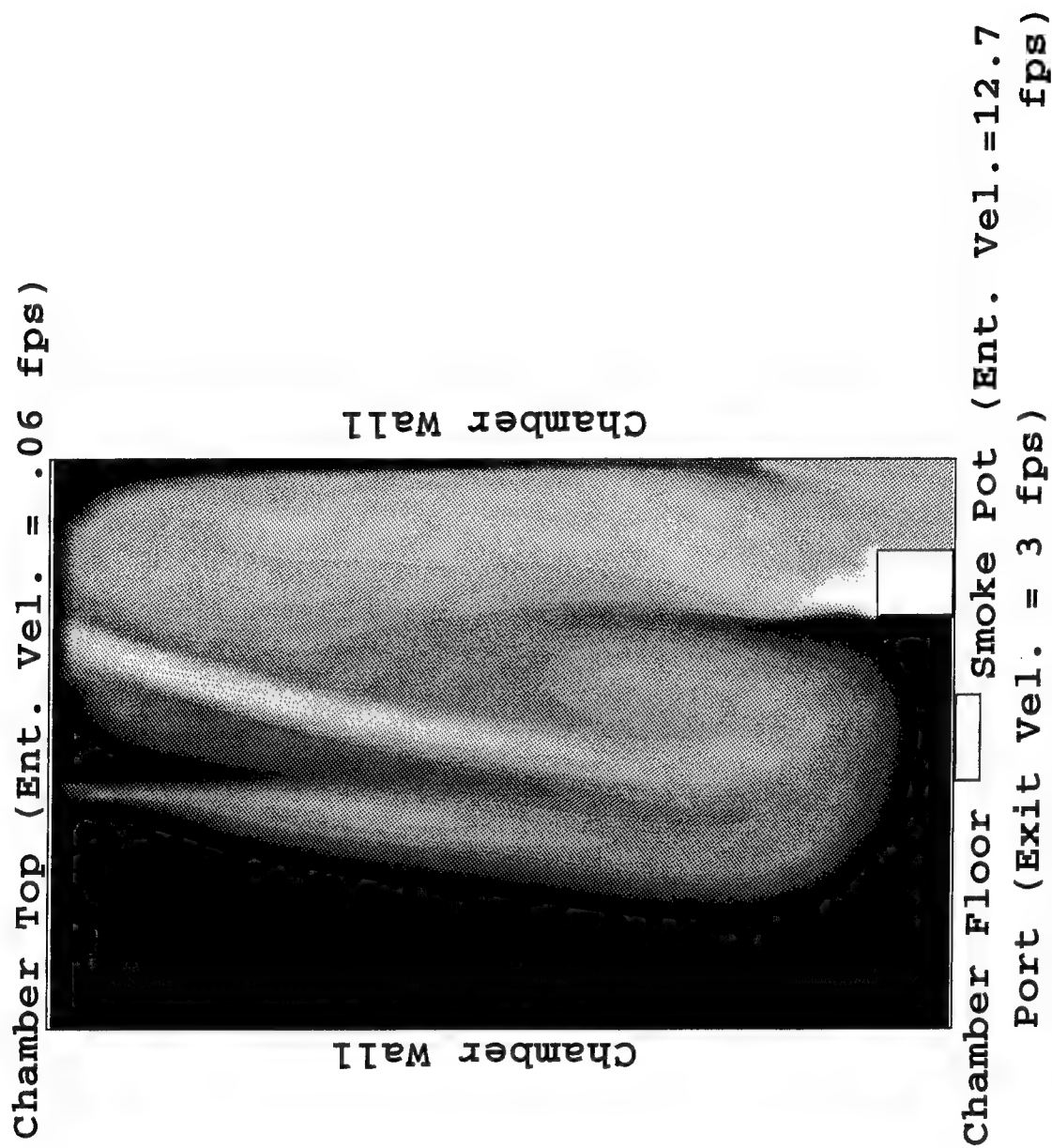


Figure 9. Effluent mass fraction contours 2.0 min after smoke pot startup.

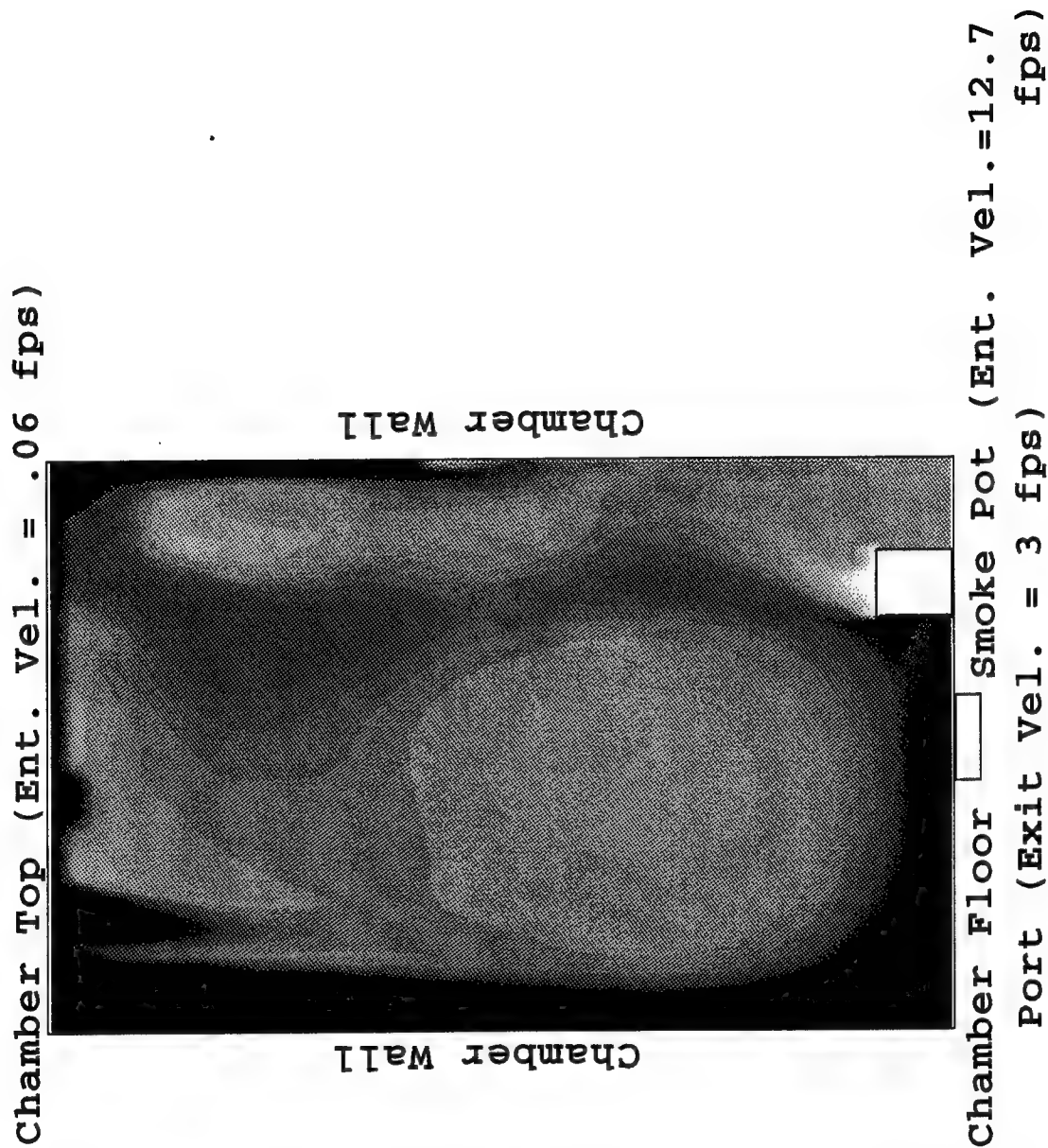


Figure 10. Effluent mass fraction contours 3.0 min after smoke pot startup.

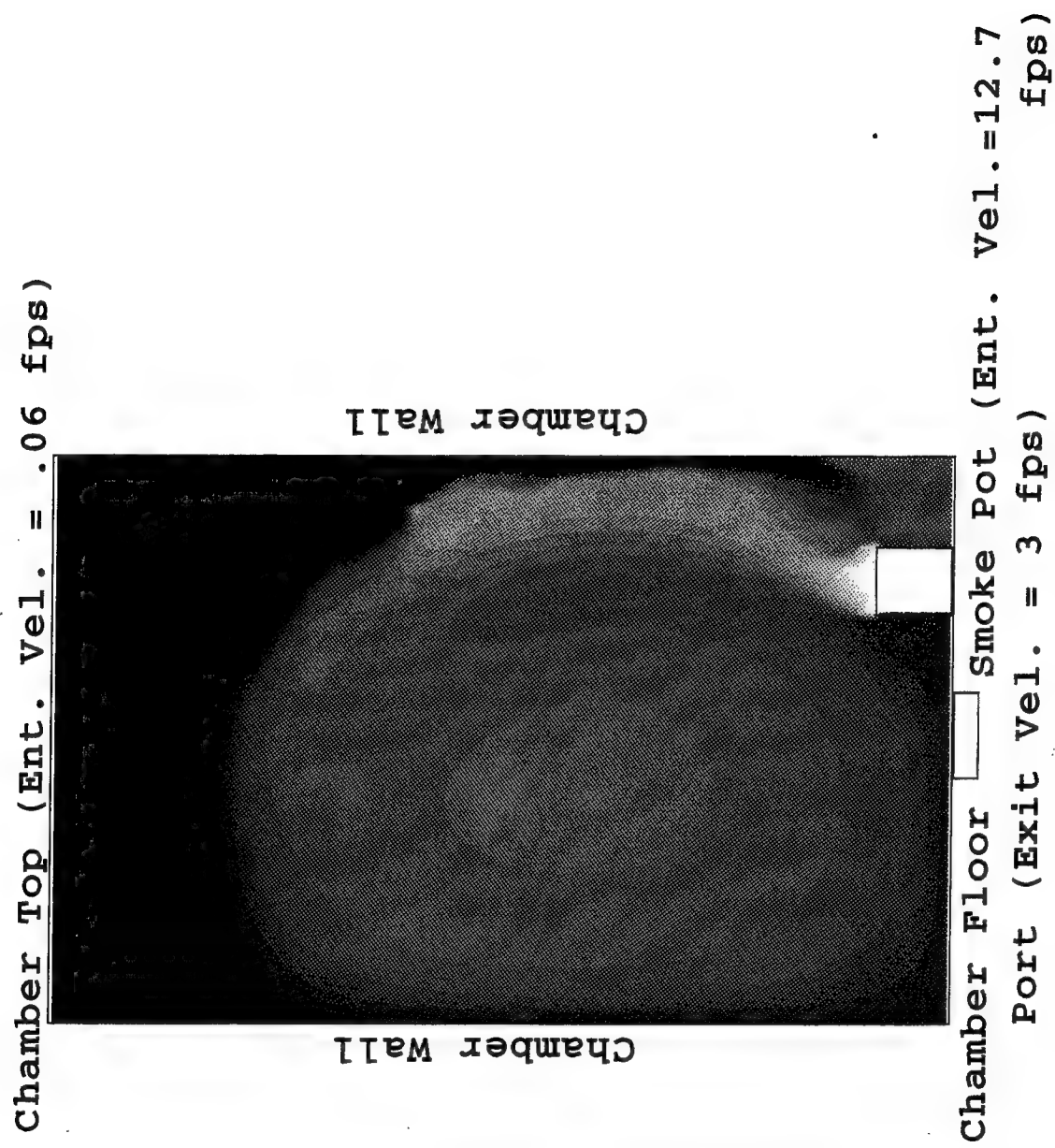


Figure 11. Effluent mass fraction contours 4.0 min after smoke pot startup.

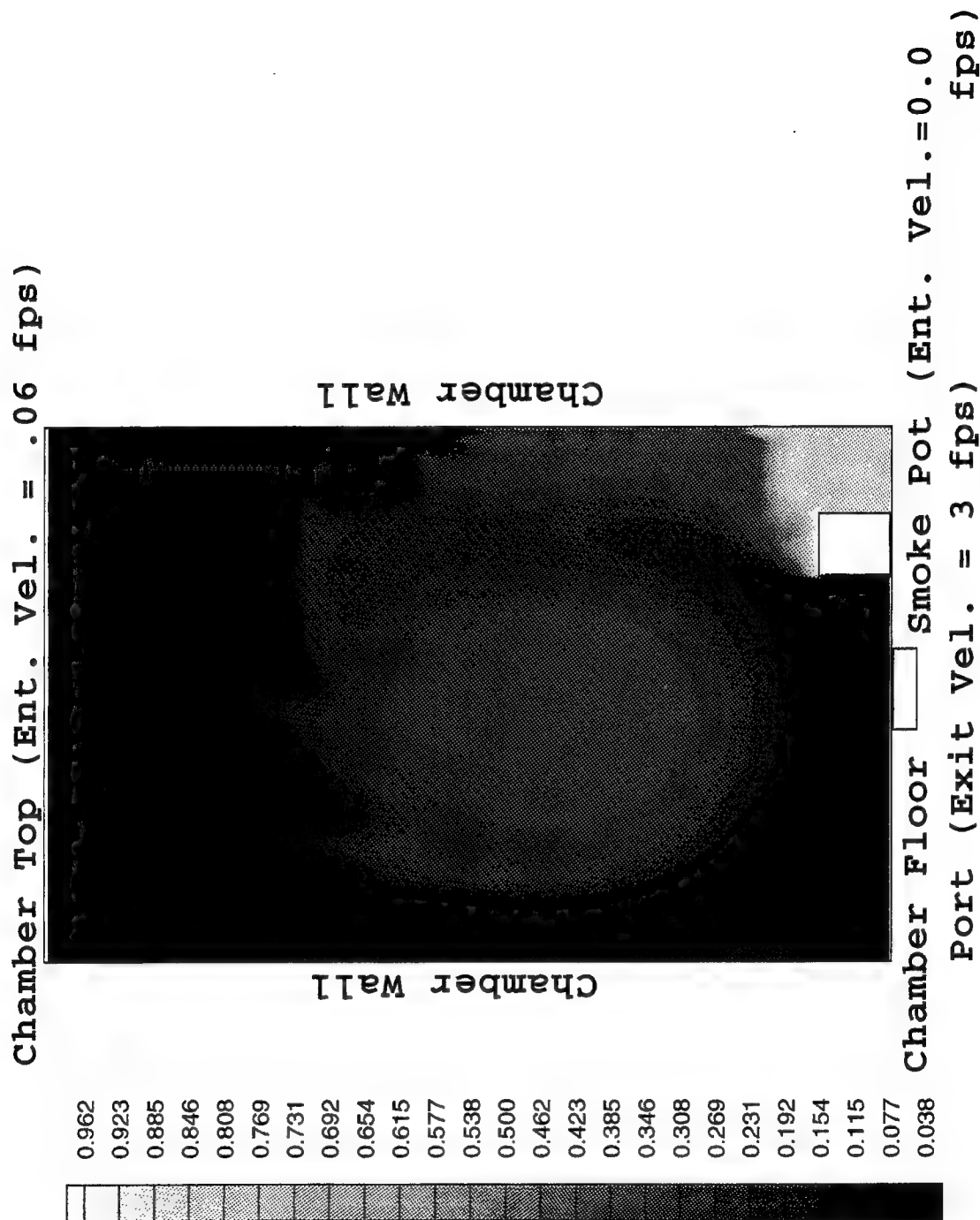


Figure 12. Effluent mass fraction contours 4.5 min after smoke pot startup, 0.5 min after smoke pot termination.

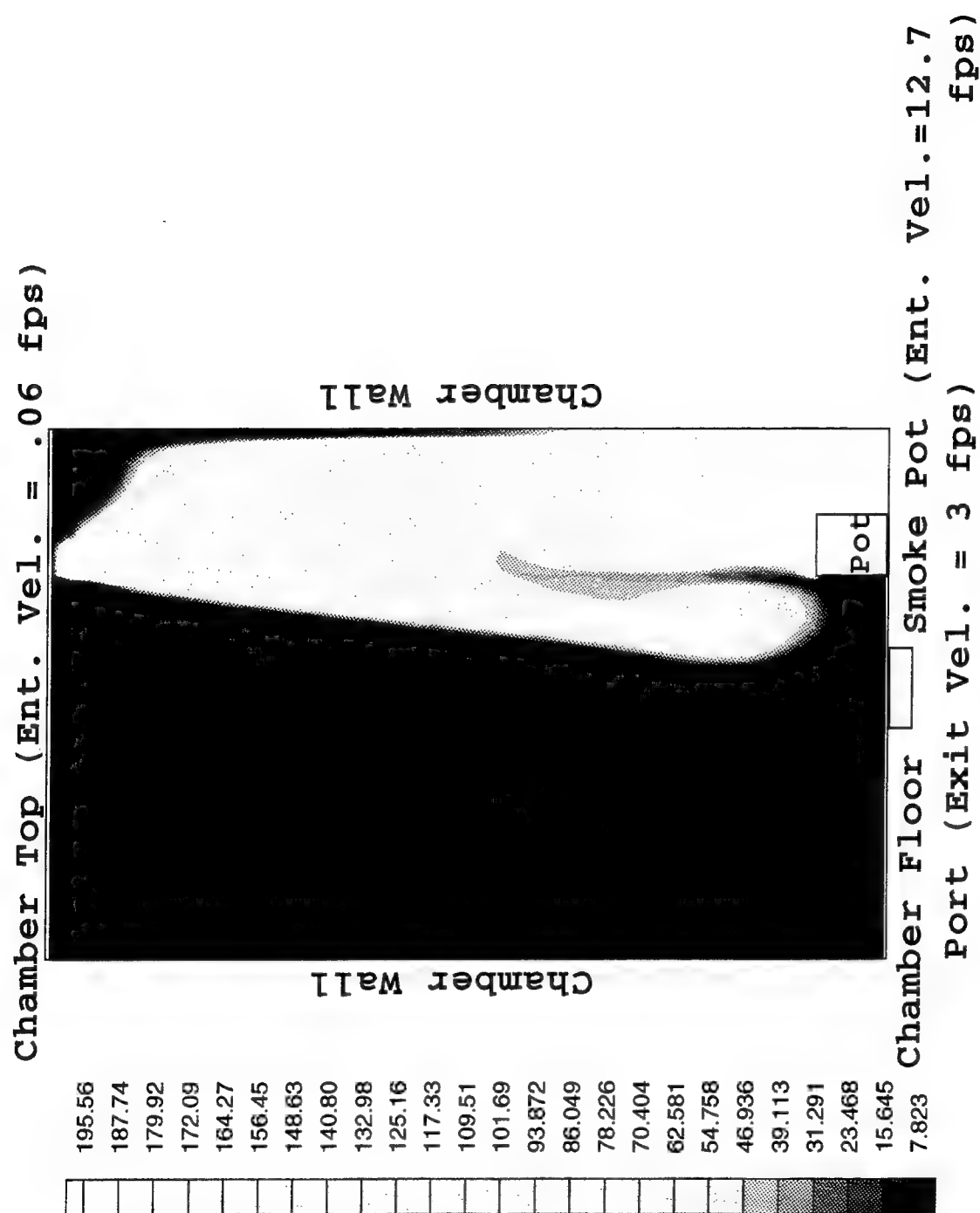


Figure 13. Effluent density ( $\text{g/m}^3$ ) contours 1.0 min after smoke pot startup.

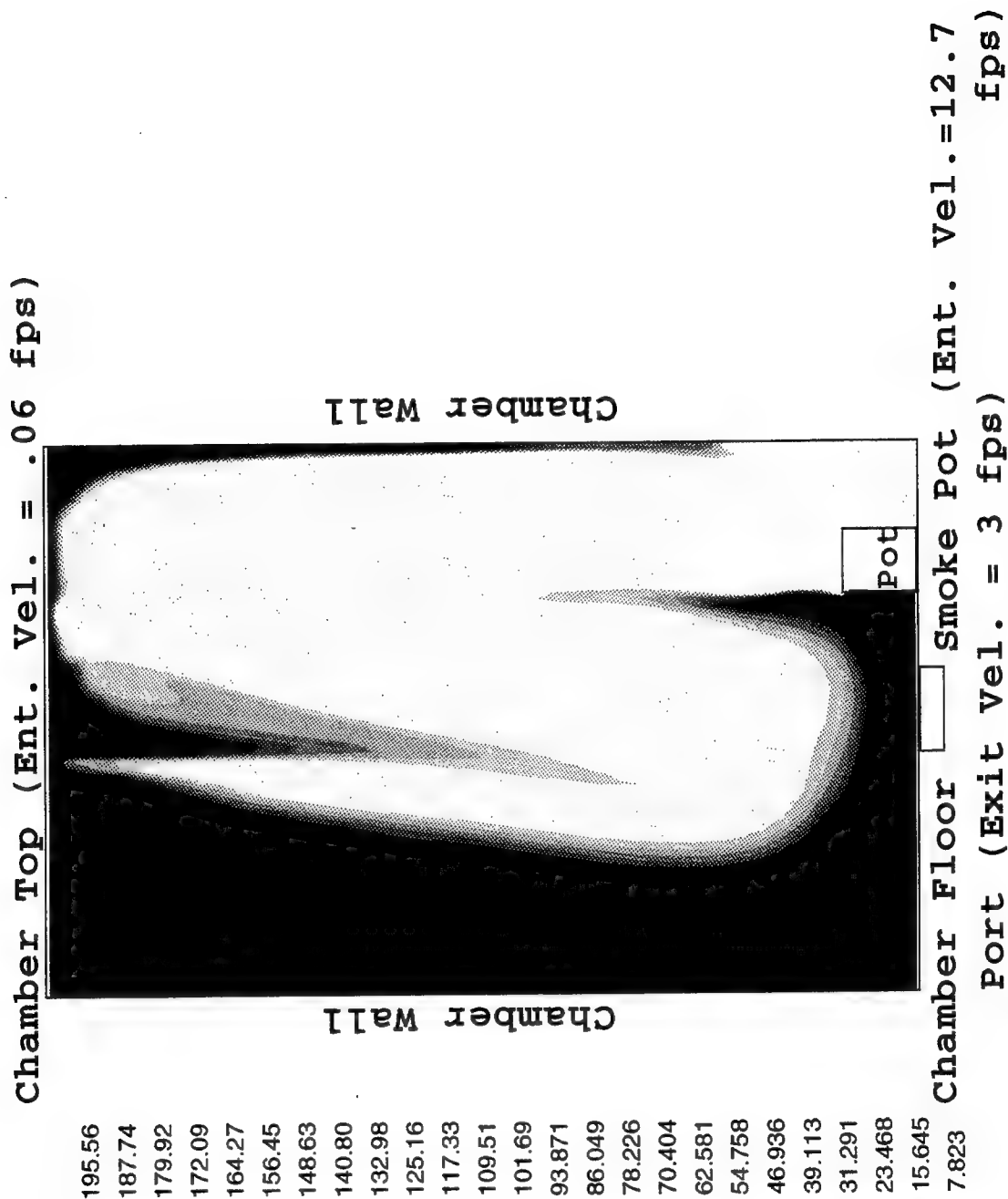


Figure 14. Effluent density ( $\text{g/m}^3$ ) contours 2.0 min after smoke pot startup.

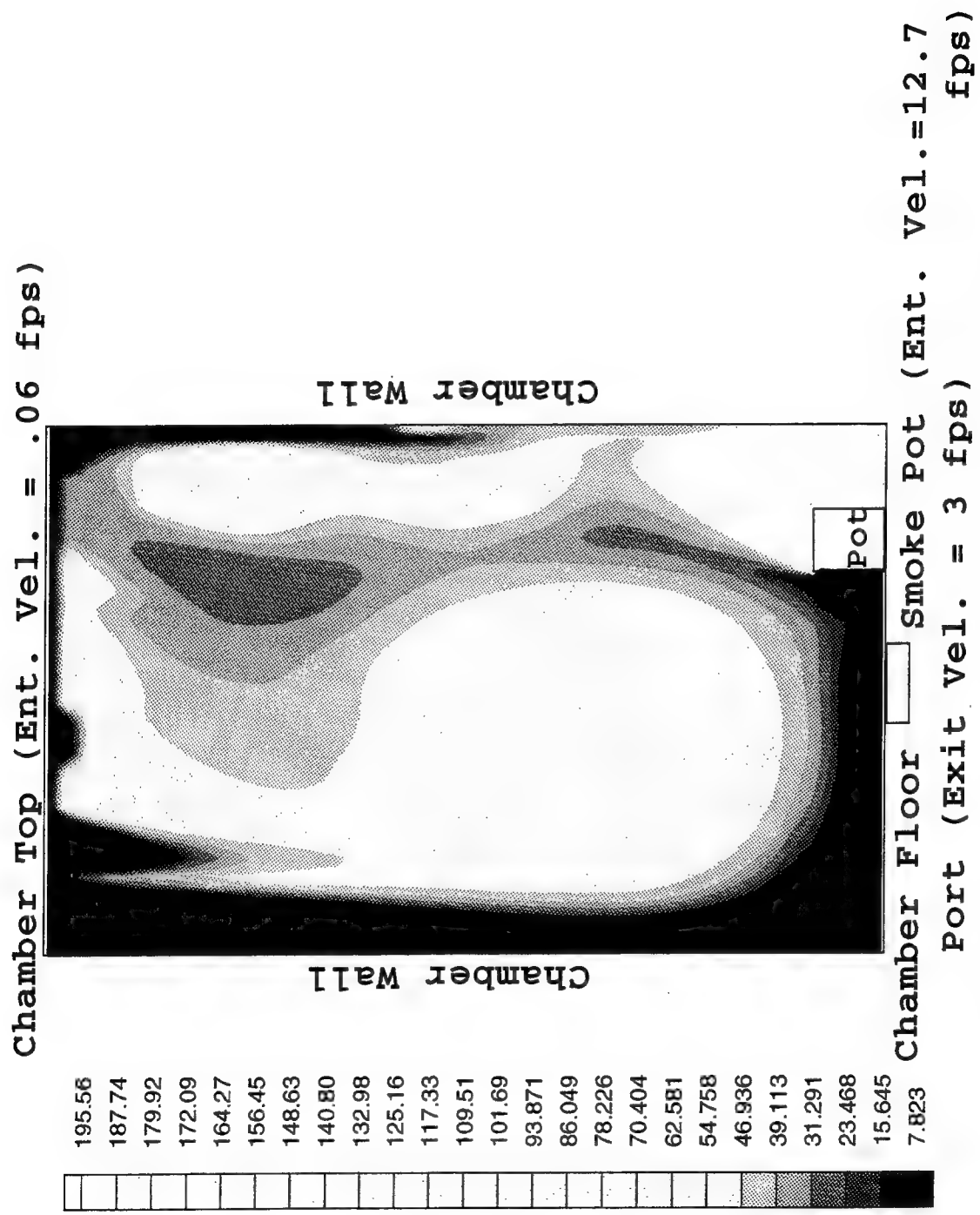


Figure 15. Effluent density ( $\text{g/m}^3$ ) contours 3.0 min after smoke pot startup.



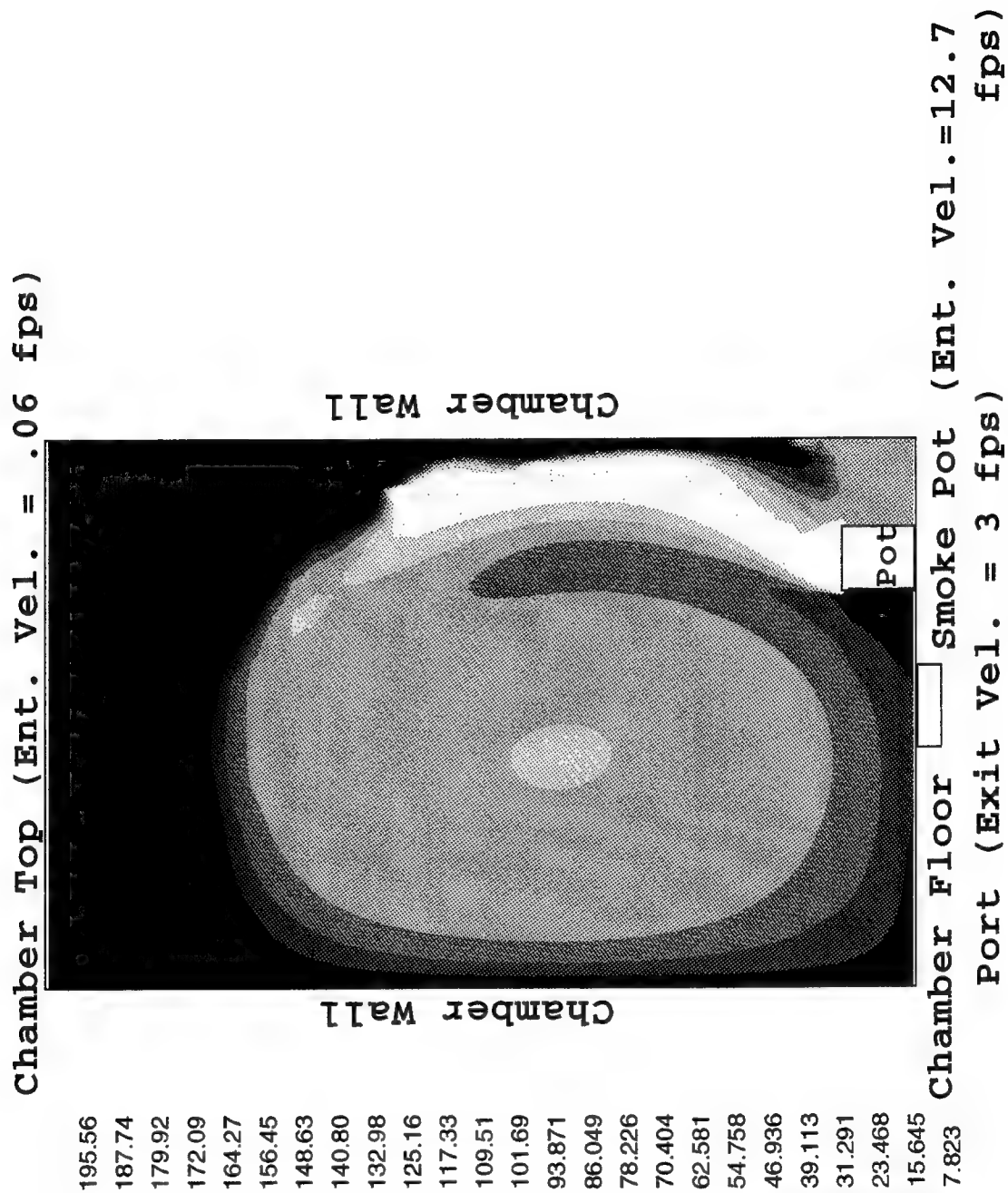


Figure 16. Effluent density ( $\text{g/m}^3$ ) contours 4.0 min after smoke pot startup.

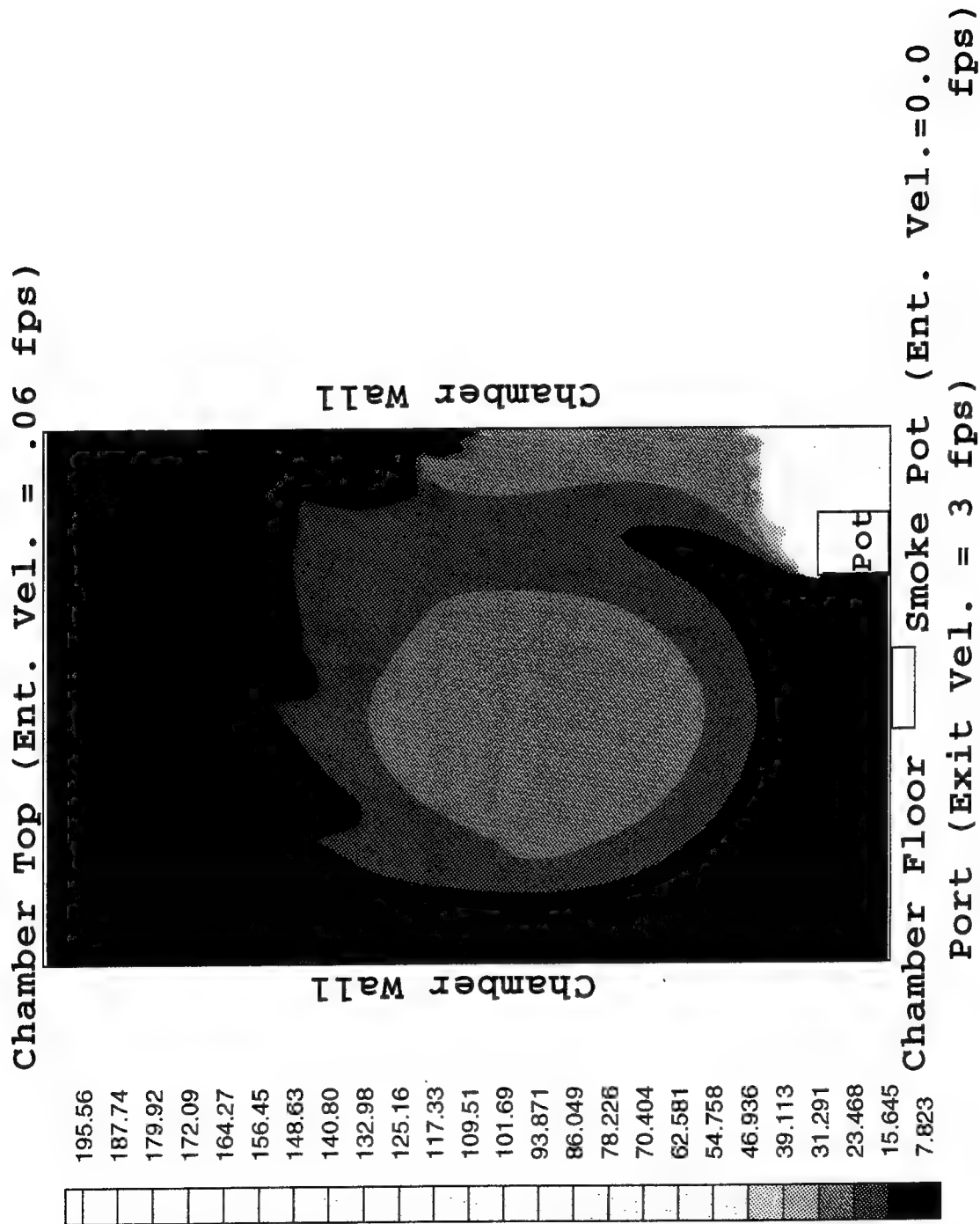


Figure 17. Effluent density ( $\text{g/m}^3$ ) contours 4.5 min after smoke pot startup, 0.5 min after smoke pot termination.

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## LIST OF SYMBOLS

$c_p$	=	specific heat capacity, constant p
$c_v$	=	specific heat capacity, constant volume
$D$	=	mass diffusion coefficient
$e$	=	specific total internal energy
$F, G$	=	flux vectors
$h$	=	molar specific enthalpy
$L$	=	Prandtl mixing length
$M$	=	molecular weight
$N$	=	total number of species
$p$	=	static pressure
$R$	=	specific gas constant, $(\gamma-1)c_p/\gamma$
$R_u$	=	universal gas constant, $R M_m$
$Sc$	=	Schmidt Number, $\mu_m/\rho D$
$t$	=	time
$T$	=	static temperature
$u$	=	axial velocity
$v$	=	radial velocity
$W$	=	dependent variable vector
$x, y$	=	Cartesian coordinates
$X$	=	species mole fraction

### Greek Symbols

$\gamma$	=	ratio of specific heats, $c_p/c_v$
$\Delta H_f$	=	enthalpy of formation
$\delta$	=	boundary layer displacement thickness
$\varepsilon$	=	boundary layer intermittency factor
$\kappa$	=	heat transfer coefficient
$\mu$	=	molecular viscosity

$\rho$	=	density
$\sigma$	=	species mass fraction
$\tau$	=	shear stress tensor
$\omega$	=	chemical production term
$\Omega$	=	source term vector

### Subscripts

e	=	edge of the viscous layer
i	=	i <sup>th</sup> species
m	=	mixture quantity
p	=	constant pressure
t	=	turbulence quantity
v	=	constant volume
x	=	x-direction
y	=	y-direction

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